

S.S.R. DEGREE COLLEGE, (AUTONOMOUS)

NIZAMABAD (C.C:5029)

I - SEMESTER INTERNAL ASSESSMENT – II EXAMINATIONS

MATHEMATICS

QUESTION BANK

I. Multiple Choice Questions

1. If the auxiliary equation has complex conjugate roots then the complementary function is _____ (A)
a) $e^{ax} (C_1 \cos \beta x + C_2 \sin \beta x)$ b) $e^{-ax} (C_1 \cos \beta x + C_2 \sin \beta x)$
c) $e^{\beta x} (C_1 \cos \alpha \beta x + C_2 \sin \alpha x)$ d) $e^{\beta x} (C_1 \cos \alpha \beta x + C_2 \sin \alpha x)$
2. The complementary function of an equation having the roots 1, 2 is _____ (B)
a) $C_1 e^x + C_2 e^x$ b) $C_1 e^x + C_2 e^{2x}$
c) $C_1 e^{-x} + C_2 e^{2x}$ d) $C_1 e^{-x} + C_2 e^{-2x}$
3. The complementary function of an equation having the roots -1, -1, 4 is _____ (C)
a) $C_1 e^x + C_2 e^x + C_3 e^{4x}$ b) $C_1 e^{-x} + C_2 e^{-x} + C_3 e^{4x}$
c) $C_1 + C_2 x + C_3 e^{4x}$ d) None
4. The G.S of nth order non homogeneous D.E is _____ (A)
a) $Y = Y_c + Y_p$ b) $y = y_c \cdot y_p$ c) $Y = y_c - y_p$ d) $Y = Y_c (1/y_p)$
5. The complementary function of an equation having the roots $2+3i$ is _____ (B)
a) $Y_c = C_1 e^{2x} + C_2 e^{3x}$ b) $e^{2x}(C_1 \cos 3x + C_2 \sin 3x)$ c) $y = y_c - y_p$ d) $y = y_c (1/y_p)$
6. The particular integral of $(D^2 - 5D + 6)y = 0$ is _____ (D)
a) 1 b) 5 c) 6 d) 0
7. The particular integral of $\frac{1}{D^2-1} \cos 3x$ is _____ (C)
a) $\frac{1}{10} \cos 3x$ b) $\frac{1}{10} \sin 3x$ c) $-\frac{1}{10} \cos 3x$ d) $-\frac{1}{10} \sin 3x$
8. The Complementary function of $(D^2 - 1)y$ is _____ (D)
a) $C_1 e^x + C_2 e^x$ b) $C_1 \cos hx + C_2 \sin hx$ c) Both (a) & (b) d) $C_1 e^{2x} + C_2 e^{2x}$
9. The particular integral of $\frac{9}{D^2+5D+4}$ is _____ (D)
a) 0 b) 1 c) $\frac{4}{9}$ d) $\frac{9}{4}$
10. The complementary function of $(D^2 + 4)y$ is _____ (A)
a) $C_1 \cos 2x + C_2 \sin 2x$ b) $C_1 \cosh 2x + C_2 \sinh 2x$
c) $(C_1 + C_2 x) e^{2x}$ d) $C_1 e^{2x} + C_2 e^{-2x}$
11. The Particular integral of $4x^2$ can be written _____ (A)
a) $AX^2 + BX + C$ b) $Ax^2 - BX + C$ c) $Ax^2 + BX - C$ d) - (A)
12. In cauchy Euler equation, 'X' is substituted as _____
a) + b) Log + c) e^+ d) None of these

13. The two linearly independent solutions of $(D^2 - 3D + 2)Y$ is (D)
 a) e^{-x}, e^{-2x} b) e^{-x}, e^{2x} c) e^x, e^{-2x} d) e^x, e^{2x}
14. If $\phi(x) = x + \log x$ by Cauchy Euler Equation $\phi(x)$ becomes (A)
 a) $e^+ + t$ b) $e^+ - t$ c) $e^+ \cdot t$ d) $t e^+$
15. In Legendre's linear equation $ax + b$ substituted as (B)
 a) $\log t$ b) e^t c) e^{-t} d) None
16. Which of the following is miscellaneous D.E (C)
 a) $\frac{d^2y}{dx^2} = f(x)$ b) $\frac{dx}{dy} = f^1(x)$ c) $\frac{d^2y}{dx^2} = f(x)$ d) None
17. Which of the following is partial differential equation (D)
 a) $\frac{\partial^2}{\partial x} = p$ b) $\frac{\partial^2}{\partial y} = q$ c) $\frac{\partial^2 z}{\partial x^2} = r$ d) All
18. The solution obtained from complete integral through assigning particular values to constants is (B)
 a) complete solution b) particular solution c) both d) None
19. If one of the solutions of differential equation is known then the second solution can be determined by using (C)
 a) method of undetermined coefficient b) variation of parameter
 c) Reduction of order method d) None of these
20. If $y_2 = y_1 \int u(x) dx$ then $u(x) =$ (B)
 a) $e^{\frac{\int f_1(x) dx}{f_2(x)}} b) e^{-\frac{\int f_1(x) dx}{f_2(x)}}$ c) $e^{\frac{\int f_2(x) dx}{f_1(x)}} d) e^{-\frac{\int f_2(x) dx}{f_1(x)}}$

II. Fill In The Blanks

- The general solution of n^{th} order homogeneous differential equation is complement function.
- The auxiliary equation $(D^2 - 3D + 2)y =$ $m^2 - 3m + 2$.
- The roots of $(D^2 - 5D + 6)y$ are 2, 3.
- If the roots of auxiliary equation are real then complementary function is $C_1 e^{m_1 x} + C_2 e^{m_2 x} + \dots$
- The particular integral for $f(D)y = e^{ax}, f(a) \neq 0$ is $e^{ax}/f(a)$
- The value of $\frac{e^{2x}}{D^2 + 4D + 3}$ is $e^{2x}/15$.
- The auxiliary equation having the roots 2, 3 is $m^2 - 5m + 6 = 0$.
- The complementary function of $(D+2)(D-2)$ is $C_1 e^{-2x} + C_2 e^{2x}$
- The particular integral of differential equations depends on $Q(x)$
- In method of undetermined coefficients $f(D)y =$ $f(D)y_p$
- If ' y_1 ' is known solution then ' y_2 ' can be determined by formula $y_2 = y_1 \int \frac{1}{y_1^2} Q(x) dx$
- By substituting $X = e^t$ Cauchy Euler equation is converted into linear equation with constant coefficients.
- The particular integral of $(D^2 + 4D + 4)y = 6e^x$ is $\frac{2}{3} e^x$
- In method of variation of parameters, the two linearly independent solutions can be determined from complementary.

15. If $Q(x) = x^2$ in Cauchy –euler equation reduced to linear order differential equation the x^2 becomes e^{2t} .
16. The two linearly independent solution of $(D^2+4D+4)y$ are e^{-2x} and xe^{-2x}
17. **Partial differential equation** can be obtained by eliminating arbitrary constants (or) arbitrary functions in valuing two or more variables.
18. The solution of first order PDE that has two arbitrary constants is called as **complete integral**.
19. The linear PDE of first order is also called as **Lagranges linear** PDE.
20. The equation of the form $\frac{dx_1}{p_1} = \frac{dx_2}{p_2} \dots\dots\dots \frac{dx_n}{p_n} = \frac{dz}{R}$ is called as **subsidiary equation**.

III. Descriptive Questions

1. Solve $(D^2+4D+4)y = 4x^2 + 6e^x$ by method of undetermined coefficient.
2. $(D^2+4D+4)y = 3x^{-2x}$ by the method of undetermined coefficient.
3. Solve $(D^2-3D+2)y = \sin^{-x}$ using the method of variation of parameter.
4. Solve $x^2 \frac{d^2y}{dx^2} - x \frac{dy}{dx} + y = 2 \log x$.
5. Solve $x^2y^{11} - xy^1 + y = 0$ given $y_1 = x$ as a solution