

**TELANGANA UNIVERSITY**  
**S.S.R. DEGREE COLLEGE, NIZAMABAD (C.C:5029)**  
**IV SEMESTER INTERNAL ASSESSMENT II EXAMINATIONS**  
**MATHS (ALGEBRA) QUESTION BANK**

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I. Multiple choice questions.

1. A homomorphism  $G \rightarrow G'$  is an isomorphism iff the kernel consists of \_\_\_\_\_ [b]  
(a) The identity 'e' only (b) A normal subgroup of G  
(c) A factor group of G (d) Inverse of G
2. If N and H are normal subgroups of a group G, then NH is \_\_\_\_\_ [a]  
(a) HN (b) H (c) N (d) None of these
3. Which of the following statements is correct? [b]  
(a) Every homomorphism is an isomorphism (b) Every isomorphism is a homomorphism  
(c) Homomorphism and isomorphism are not related (d) None of these
4. If N is a normal subgroup of a group G and  $a \in G$  then [d]  
(a)  $Na \cap aN = \emptyset$  (b)  $Na < aN$  (c)  $Na \neq aN$  (d)  $Na = aN$
5. For any two elements a, b in a ring,  $a(-b) =$  [a]  
(a)  $-(ab)$  (b)  $ab$  (c)  $-(ba)$  (d) None of these
6. If  $(R, +, \cdot)$  is a ring then  $(R, +)$  is [b]  
(a) A group (b) An abelian group (c) A finite group (d) Semi group
7. The residue classes modulo 11 with respect addition and multiplication modulo 11 is [d]  
(a) Commutative ring (b) An integral domain (c) Skew field (d) A field
8. The characteristic of the residue classes mod 8 is \_\_\_\_\_ [c]  
(a) 0 (b) 2 (c) 8 (d) 3
9. With the usual addition and multiplication, the set of all even integers is [a]  
(a) A ring (b) A field (c) An integral domain (d) A sub ring
10. If  $S_1, S_2$  are two subrings of a ring R, then  $S_1 + S_2$  is [c]  
(a) Subring (b) Ideal (c) Need not be a subring (d) Not a subring
11. If F is a field, then the number of ideals in F is \_\_\_\_\_ [c]  
(a) 0 (b) 1 (c) 2 (d) Infinite
12. A subring S of a ring R is called ideal if [c]  
(a)  $\alpha \in S, a \in R \Rightarrow \alpha a \in S$  (b)  $\alpha \in S, a \in R \Rightarrow a\alpha \in S$   
(c)  $\alpha \in S, a \in R \Rightarrow \alpha a, a\alpha \in S$  (d) None of these
13. If R is a non-zero ring so that  $a^2 = a \forall a \in R$  then characteristic of R = [d]  
(a) Prime (b) 0 (c) 1 (d) 2
14. For the homomorphism  $f: R \rightarrow R$  defined by  $f(x) = x \forall x \in R$  Ker f = \_\_\_\_\_ [a]  
(a)  $\{0\}$  (b) R (c)  $\{0,1\}$  (d) (d) None of these

15. If  $f(x), g(x)$  are two non-zero polynomials over a ring  $R[x]$  then  $\deg \{f(x)+g(x)\}$  is [b]  
 (a)  $= \deg f(x) + \deg g(x)$  (b)  $\leq \max \{\deg f(x), \deg g(x)\}$   
 (c)  $\geq \max \{\deg f(x), \deg g(x)\}$  (d) None of these

16. If  $f(x)=2+4x+2x^2, g(x)=2x+4x^2$  over the ring  $(I, +_6, \times_6)$  then  $\deg \{(fx)+g(x)\}=$  [d]  
 (a) -1 (b) 1 (c) 2 (d) 0

17. Every ring of numbers with unity is \_\_\_\_\_ [a]  
 (a) Integral domain (b) Division ring (c) Field (d) None of these

18. Homomorphic image of an integral domain is \_\_\_\_\_ [c]  
 (a) A ring (b) Integral domain  
 (c) Need not be integral domain (d) None of these

19. A finite integral domain is \_\_\_\_\_ [a]  
 (a) Field (b) Ring (c) Group (d) None of these

20. A field is a \_\_\_\_\_ [c]  
 (a) Non commutative ring (b) Division ring  
 (c) Commutative division ring (d) None of these

## II. Fill in the Blanks

- To determine the quotient group  $G/N$  of a group  $G$ ,  $N$  must be a normal group of  $G$ .
- The kernel of homomorphism of a group is a normal group
- Any subgroup of a cyclic group is a normal subgroup of the group of cyclic
- The alternating group is a normal subgroup of the symmetric group  $S_n$
- If  $R$  is a ring without zero divisors then cancellation laws hold in  $R$ .
- A ring  $R$  has no zero divisors if there exist  $a, b \in R$  and  $ab = 0 \Rightarrow a = 0$  or  $b = 0$
- A division ring has no zero divisors divisors.
- In a ring  $R$  if  $a^2 = a$  for  $a \in R$  'a' is called idempotent element w.r.t multiplication.
- If characteristic of a ring  $R=2$  and  $a, b \in R$  commute then  $(a-b)^2 = \underline{a^2 + b^2}$
- A subring of  $(Z_6, +_6, \times_6)$  is  $\{\bar{0}, \bar{3}\}$
- The union of two ideals of a ring  $R$ , need not be an ideal of  $R$ .
- For the ring of integers any ideal generated by prime integer is a maximal ideal
- A maximal ideal of the ring of integers is generated by prime integer
- If  $U$  is a maximal ideal of the ring  $R$  then there exists no ideal  $U'$  of  $R$  such that  $U \subset U' \subset R$
- A finite integral domain is a field
- In the quotient ring  $R/U$  the zero element is and the unity element is  $U, 1+U$
- For a commutative ring  $R$ , with unity if  $U$  is a maximal ideal then  $R/U$  is a field
- If  $f: R \rightarrow R'$  is a ring homomorphism then  $\text{Ker } f$  is an ideal of  $R$
- Every non-zero element of a field is a unit
- If  $z[i] = (a+bi \mid a, b \in z)$  then the ring is called ring of Gaussian integers

## Short Answers.

- State first isomorphism theorem?
- Mention three properties of rings?
- What is an idempotent element?
- Define an integral domain?
- What is a nilpotent element?
- Find the principal ideal generated by  $3 \in Z$ ?
- Define prime ideal?
- Define ring homomorphism?

9. State first isomorphism theorem?
10. Give two examples of prime fields?