

**TELANGANA UNIVERSITY**  
**S.S.R. DEGREE COLLEGE, NIZAMABAD (C.C:5029)**  
**III SEMESTER INTERNAL ASSESSMENT I EXAMINATIONS**  
**MATHEMATICS (REAL ANALYSIS) QUESTION BANK**

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I. Multiple choice questions.

1. The sequence  $\left[ \frac{(-1)^n}{n} \right]$  is [a]
  - a. Convergent
  - b. Divergent
  - c. Oscillatory
  - d. None of these
2. Every monotonically increasing sequence which is not bounded above diverges to [b]
  - a.  $-\infty$
  - b.  $+\infty$
  - c. 0
  - d.  $\varepsilon$
3. If  $\langle f_n \rangle$  and  $\langle S_n \rangle$  are Cauchy sequences. Then [d]
  - a.  $\langle f_n + S_n \rangle$  is a Cauchy sequence
  - b.  $\langle f_n - S_n \rangle$  is a Cauchy sequence
  - c.  $\langle f_n S_n \rangle$  is a Cauchy sequence
  - d. All the above
4. If  $\lim s_n = k$  and  $\lim t_n = l$  then [d]
  - a.  $\lim(s_n - t_n) = k - l$
  - b.  $\lim(s_n t_n) = k l$
  - c.  $\lim\left(\frac{s_n}{t_n}\right) = \frac{k}{l}$
  - d. All the above
5. The sequence  $(1+(-1)^n/n)$  is [a]
  - a. Convergent
  - b. Divergent
  - c. Oscillatory
  - d. None of these
6. For a sequence of positive real numbers  $S_n$ ,  $\lim S_n = +\infty$  if and only if [a]
  - a.  $\lim (1/S_n) = 0$
  - b.  $\lim (1/S_n) = +\infty$
  - c.  $\lim (1/S_n) = -\infty$
  - d.  $\lim (1/S_n) = a, (a \text{ is finite})$
7. If  $s_n$  be a sequence, then  $\limsup s_n$  is define as [b]
  - a.  $\lim_{n \rightarrow \infty} \sup\{s_n : n < N\}$
  - b.  $\lim_{n \rightarrow \infty} \sup\{s_n : n > N\}$
  - c.  $\lim_{n \rightarrow \infty} \inf\{s_n : n < N\}$
  - d.  $\lim_{n \rightarrow \infty} \inf\{s_n : n > N\}$
8. If  $s_n$  be a sequence then,  $\liminf \left| \frac{s_n + 1}{s_n} \right|$  \_\_\_\_\_  $\liminf |s_n|^{1/n}$  [a]
  - a.  $\leq$
  - b.  $\geq$
  - c.  $=$
  - d.  $\neq$
9. For  $p > 0$ ,  $\lim_{n \rightarrow \infty} \left[ \frac{1}{n^p} \right] =$  [b]
  - a. 1
  - b. 0
  - c.  $+\infty$
  - d.  $-\infty$
10. For a sequence  $s_n$  in  $\mathbb{R}$ , if  $S$  is a set of sub sequential limits of ' $s_n$ ' then [c]
  - a.  $\sup s = \limsup s_n$
  - b.  $\inf s = \liminf s_n$
  - c. Both a & b
  - d. Neither a nor b
11. The natural domain of  $f(x) = \sqrt{4-x^2}$  is [b]
  - a.  $\{x \in \mathbb{R} : x \neq 0\}$
  - b.  $[-2,2]$
  - c.  $[0,1]$
  - d.  $[-1,1]$
12. If  $f$  and  $g$  are real valued functions then,  $\max (f,g)(x) =$  [d]
  - a.  $f(x)+g(x)$
  - b.  $f(x)g(x)$
  - c.  $\frac{f(x)}{g(x)}$
  - d.  $\max \{f(x),g(x)\}$
13. If  $f$  and  $g$  are real-valued functions then  $\min (f,g) =$  [a]
  - a.  $\frac{1}{2}(f+g) - \frac{1}{2}|f-g|$
  - b.  $-\max(-f, -g)$
  - c.  $\frac{1}{2}(a+b) + \frac{1}{2}|a-b|$
  - d. None
14. If  $(s_n)$  and  $(t_n)$  are sequences in  $(a,b)$  that converges to 'a' then [a]
  - a.  $\lim f(s_n) = \lim f(t_n)$
  - b.  $f(a) = \lim f(s_n)$
  - c.  $\lim f(s_n) \neq \lim f(t_n)$
  - d. None
15. If  $f(x) = \frac{1}{x^2}$  then  $f'(x) =$  [d]
  - a.  $\frac{-1}{x^2}$
  - b.  $\frac{1}{x}$
  - c. 0
  - d.  $\frac{-2}{x^3}$
16. The domain of  $f(x) = \frac{x^2 - 4}{x - 2}$  is [a]
  - a.  $(-\infty, 2) \cup (2, \infty)$
  - b.  $\mathbb{R}$
  - c.  $s = (-\infty, b)$
  - d.  $(\infty, 2)$
17. The domain of  $\text{gof}$  is [b]
  - a.  $\{x \in \text{dom}(f) \cap x \in \text{dom}(g)\}$
  - b.  $\{x \in \text{dom}(f); f(x) \in \text{dom}(g)\}$
  - c.  $\text{dom}(f) \cap \text{dom}(g)$
  - d.  $\mathbb{R}$

18. Mean value theorem is given as

a.  $f(x) = y$                       b.  $f'(x) = \frac{f(x)}{g(x)}$                       c.  $f(x) = g(x)$                       d.  $f'(x) = \frac{f(b) - f(a)}{b - a}$  [d]

19.  $\lim_{x \rightarrow 1} \frac{\sqrt{x} - 1}{x - 1} =$  [d]

a. 1                      b.  $\frac{-1}{2}$                       c. 0                      d.  $\frac{1}{2}$

20. The function  $f(x) = x^2$  is uniformly continuous on [a]  
a.  $[-7,7]$                       b.  $[7,7]$                       c.  $(0,7)$                       d.  $(-7,7)$

II. Fill in the blanks

1. Every convergent sequence is bounded

2. Every Cauchy sequence is bounded

3. A sequence converges if and only if it is a Cauchy sequence

4.  $\lim s_n = k$  and  $\lim t_n = l$  then  $\lim (s_n + t_n) = \underline{k + l}$

5. If  $\langle s_n \rangle = l$  and  $\langle f_n \rangle = m$ , then  $\lim \langle s_n + f_n \rangle = \underline{l+m}$

6. If  $s_n$  is unbounded increasing sequence then  $\lim s_n = \underline{+\infty}$

7. If  $s_n$  converges to  $s$ , then its subsequence  $s_{n_k}$  converges to same limit i.e.,  $s$

8.  $\sum \frac{1}{n} = \underline{+\infty}$

9. If  $(s_n) \rightarrow s$  and  $(t_n)$  is any sequence then  $\limsup s_n t_n = s \cdot \limsup t_n$

10. Every bounded sequence has convergent subsequence

11. The set on which  $f$  is defined is called the domain

12. The function  $f$  is said to be continuous if it is continuous on dom(f)

13. If  $f$  and  $g$  are continuous at  $x_0$  in  $\mathbb{R}$ . Then  $\max(f,g)$  is continuous at  $x_0$

14. A real valued function  $f$  is said to be bounded if  $\{f(x) : x \in \text{dom}(f)\}$  is a bounded set

15. If  $f$  is uniformly continuous on a closed and bounded set  $S$ , then  $f$  is uniformly continuous

16. A function  $f$  is continuous in  $\text{dom}(f) = s$  if and only if  $\lim_{x \rightarrow a^s} f(x) = f(a)$

17. If  $f$  is uniformly continuous on a set  $S$  and  $(s_n)$  is a Cauchy sequence in  $S$  then  $(f(s_n))$  is a Cauchy sequence

18. A function  $\bar{f}$  is an extension of a function  $f$

19. If  $f$  and  $g$  are real-valued functions, then  $\min(f,g)(x) = \underline{\min\{f(x), g(x)\}}$

20. The domain of  $\frac{f}{g}$  is the set  $\text{dom}(f) \cap \{x \in \text{dom}(g) : g(x) \neq 0\}$

III. Short Answers.

1. Define Convergent sequence.

2. Define Monotone sequence.

3. Define Cauchy sequence.

4. State Alternating series theorem.

5. State Integral test.

6. Define Continuous function.

7. Define Uniform continuous function.

8. Define Sub sequence.

9. Define Limit of a function.

10. Define Limit Inferior and Limit superior.